

Peer Review

Review of: "Aspects of a Randomly Growing Cluster in $\mathbb{R}^2$, $d \geq 2$ "

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The paper studies a particular model for a set of random points. The mathematical arguments presented in the paper are rigorous and well-founded, though some details require clarification (see Comments below). Additionally, the authors should provide a clearer motivation for why this particular model is chosen. Do the authors have a specific application in mind for their model?

*** Comments:

1. The notation $N(0, \sigma)$ is ambiguous, as it is unclear whether σ represents the variance or the standard deviation. Later, it becomes evident that it denotes the standard deviation. However, it is more common for the second argument in $N(.,.)$ to represent the variance, typically written as σ^2 . Therefore, some clarification is needed.
2. In the definition of $\rho(X)$ on p. 1, use $\sup$ instead of $\max$ because the maximum of an infinite set is not necessarily attained.
3. The symbol $\pi(i)$ on the first line of Chapter 2 is not defined.
4. When referring to [2] on p. 2, Chapter 14.2 should be rather Chapter 15.2 in the online version of the book.
5. The symbol $[k_1, k_2]$ on p. 3 is not defined.
6. The symbol $\text{dist}(i)$ on p. 3 is not explained.

7. At the beginning of Subsection 3.2, the first bound needs some clarification. I would expect $|N(0, i^{\{-\alpha\}}) - N(0, j^{\{-\alpha\}})|$ instead of $|N(0, m^{\{-\alpha\}}) - N(0, m^{\{-\alpha\}})|$.

Moreover, the next equality is not correct as $N(0, m^{\{-\alpha\}}) - N(0, m^{\{-\alpha\}})$ is $N(0, \sqrt{2} * m^{\{-\alpha\}})$ if the second argument of $N(.,.)$ stands for the standard deviation.

8. In classical point process theory, a point process has finitely many points in every bounded set. In this sense, the proposed model is not a point process, as stated in the first line of the Summary.

*** Minor comments (formulas):

Eq. (1): It would be better to use $\lambda_m(i)$ rather than $\lambda(i)$ to stress the dependence on m .

Eq. (3): The term $d^{\{1/2\}}$ is missing on the right-hand side.

*** Minor comments (language):

Introduction, l. 11: a the set -> the set

p. 2, l. 4: is grows -> grows

Chapter 2, l. 2: to to -> to

p. 5, 3 times: Eggenburger -> Eggenberger

*** Minor comments (typography):

Abstract, l. 2: Do not write a comma and period after an ellipsis (...).

Introduction, l. 2: Do not write a comma after an ellipsis (...).

Introduction, l. 11: Do not write a period after an ellipsis (...).

Theorem 2: Use a slanted version of L_n instead of a crossed one.

Section 3.2.1, l. 4: nrounds -> n rounds

*** Minor comments (references):

[1]: journal volume (31) and pages are missing

[3]: 200 -> 2000

[5]: It is not necessary to capitalize the first letters of the paper's title.

Declarations

Potential competing interests: No potential competing interests to declare.