

Beam Leakage: Does Polarization (of Positron) Optimize? More on Accelerators too?

Hani W. Maalouf Physics Department Lebanese University
Faculty of Science II Fanar Lebanon

Abstract: An Instrumental trial based on theory of gluons pre-quenching is proposed to resolve some of the beam deficiencies (low systematics and high spilling's in the various steps) especially here the positron polarization. The idea can be used too maybe to reduce the size of accelerators as crucial in concordance after recounting such leak or by the technical rounding improvements.

Introduction

The presence of lines in the accelerators' beams were discovered recently, [1].

Here a theorist effort to improve at least one instrumental effect, as also can be (on the side of) for experimental recycling and recollection of data to break the next new physics barriers.

Specifically, one may think in terms of the coherent mini-sub-beams spilled out of the main beam in the running energy ranges, well and up till around 100 GeV, so then passing the Electroweak scale into the BSM thresholds, represented by another Higgs, noted pseudo-scalar noted by indices 1 and 2, in the Appendix.

Also more ruining may come out due to the non-elimination of the processes especially the CP violating ones by the external magnetic field at very low diffusion angles as they diffuse almost along the beam axis and can escape also their reversion.

These sub-beams develop from the gluons which originate from the Higgs background decaying into γ and Z with the last re-decaying into gluons.

The gluons are known of making jets' quenching above certain angle, leading that a spilling of frequencies ω_c at a smaller than an angle θ_s .

That should satisfy a longitudinal double-flux variation such that, after integration in the 2nd equation,

$$2\omega_s = sL^2 \Rightarrow 2\Delta N_x^D = \frac{sL^3}{3} \Rightarrow \Delta N^D = sL^3/2$$

Where the superscript D relates to double.

But a double of a single flux can be made from the turn of one side of a turn so $\Delta N^D = 2\Delta N\Delta N$

$$\theta_s = \frac{1}{\Delta N} = \frac{1}{\sqrt{\frac{\Delta N^D}{2}}} = \frac{2}{\sqrt{sL^3}}$$

The length L is characteristic for the nuclear matter.

While s is a collective screening due to a lattice of pure quark valence parameter just close to the inside of the nucleon so then its range of interaction with the Gluons energy is the same as the Debye length. To deduce, up to constant, that

$$s = \frac{q^2}{l}$$

Where q is the elementary charge of the nucleon, and l is the Debye Length, [2].

This integration allows a direct resolution as if there is a hidden transverse dimensional link that allowed the contact between the two fluxes.

In nuclear forces this is a Yukawa type force which is exactly what gave the benchmark which links, as worked out in the Appendix, an internal mass order to the charge of the type

$$q = \lambda m$$

Where λ is of the order of a Yukawa coupling being approximated by $\frac{Y'^{1st \text{ gen}}_{\text{Yukawa}}}{(\lambda_{EW})^{\frac{1}{2}}}$, so an estimate of

$$Y'^{1st \text{ gen}}_{\text{Yukawa}} \approx 0.16 Y'^{2nd \text{ gen}}_{\text{Yukawa}} \approx (0.16)^2 Y'^{3rd \text{ gen}}_{\text{Yukawa}} \quad \text{While } Y'^{3rd \text{ gen}}_{\text{Yukawa}} \approx \lambda' Y'^{3rd \text{ gen}}_{\text{Yukawa}}$$

Where $Y'^{3rd \text{ gen}}_{\text{Yukawa}} \sim 1$ with $\lambda' \sim \lambda^2$ is the self- coupling in the extended Higgs.

Since the Debye occurs at the valence quark inside the nucleon and these constitutes a less than 1 per cent of the nucleon mass.

The order of the Yukawa is small so is expected being of the order of 10^{-2} at best.

Then too, the mass m has the order of few hundreds of a Nucleon, being associated with the link size reaching up to the restoration energy, (Here EW vacuum energy).

Writing the quenching parameter in the new link parameters

$$\theta_s^2 = \frac{4}{sL^3} = \frac{4}{\left(s\left(\frac{2\omega_s}{s}\right)^{\frac{3}{2}}\right)} \Rightarrow \theta_s^4 = \frac{4^2 s}{(2\omega_s)^3} = \frac{2\lambda^2 m^2}{l\omega_s^3}$$

$$\Rightarrow \theta_s \cong 1.2\lambda^{\left(\frac{1}{2}\right)} \left(\frac{L_s^3}{L_m^2 l}\right)^{\frac{1}{4}}$$

In values $L_s = 1 \text{ GeV}$, $l \sim 0.1 \text{ MeV}$ and $L_m = 150 \text{ GeV}$

$$\theta_s \cong 1.2\lambda^{\frac{1}{2}} \left(1 \times \frac{1 \times 10^4}{(1.2)^2 \times 10^4}\right)^{-\frac{1}{4}} \approx 1.3\lambda^{\frac{1}{2}} = 1.3 \times \left[(0.16)^2 (0.1)^{2-\frac{1}{2}}\right]^{\frac{1}{2}}$$

$$= 1.4 \times 0.16 \times 0.18 \cong 0.028 \sim \frac{\theta_{\text{spilling}}}{2} \approx \frac{0.05}{2} = 0.025$$

Where $\theta_{\text{leak}} \cong 5\%$ is the cited value for the ruining beam leak, [1].

As a centering of an angle θ_s with respect to the cylindrical axis would simply lead to its doubling, making it so of a value that compares easily to be leaking.

In terms of the parameters, since L_s and L_m are fixed what is left

$$\theta_s \propto \frac{\lambda^{\frac{1}{2}}}{l^{\frac{1}{4}}}$$

So decreasing the Debye energy by a factor of 20 would lead to decrease of the angle by a factor of 2.5 however such a decrease of scattering would correspond to a high lowering of the energy of the system so if its Yukawa's are expected also to be heightened by an almost 10 so same outcome is on the side of low energy.

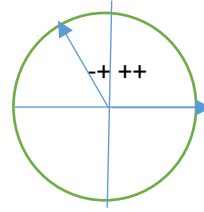
For the high energy the Yukawa since dealing with the low quarks are stabilized while if the Debye will increase by factor of 2 up to 10 then the increase of the spilling beam angle is by a factor of 1.2 up to 1.8.

Therefore a direct improvement is not much feasible in the regions where there is a clear separation between the gluons Debye and the Yukawa of the quarks.

Impact of the Boundary Conditions: Gaining the Polarization of the Positron

Under isotropic beams' conditions, the beam surface is supposed to be the gauge matching region.

If one assumes that the beams surfaces are roughly circular then since leaks is partial on the circumference and the fusion-disintegration play a role between various spilling's so a matching in-between is the concluded boundary condition.



Since three directions are free to spill then an isotropic angle is the 120° .

However, forgetting about the longitudinal beam leakage matching since it goes along the beam itself.

Its matching is then between k_x and k_y such that is their signatures that goes along or not, (as due the Poincare circle available gauge that is here the Mobius one, [3], however restricted to the line of the circumference with turns one with equal signs and another with different signs).

And since the signs of k_x and k_y are distributed along the different circular quadrants. One fixes the equal signs at the 1st quadrant and at the end should multiply by 4 being the 1st turn.

A 2nd turn is at the 2nd quadrant , and plus signs are not specified in the transverse directions

Therefore, the 2nd quadrant is re-divided into 4 possible alternances of signs, to be deducing that the coherence (or Polarization ratio p_{e+}) is proportional to

$$p_{e+} = 4 \left[\frac{11}{34} + \left(\frac{11}{34} \right)^2 + \dots \right] = \frac{1}{3} \frac{1}{1-1/12} = \frac{4}{11} = 0.36$$

If the k_z are also randomly collected like e.g. if from a Bremsstrahlung production this polarization would double so

$$p_{e^+}^{\text{Brems}} = 8 \frac{\frac{1}{12}}{1 - \frac{1}{12}} = 0.72$$

That would be the case [4], if the source jets were restricted to be less than $\theta_s \approx 0.03$.

Another case is the beams created from the impact of Laser, [5], here the configuration is conical so the factor number to the circular one, since it would have an opposite angle is $3/2$, then

$$p_{e^+}^{\text{Laser}} = \frac{3}{2} \left(4 \frac{\frac{1}{12}}{1 - \frac{1}{12}} \right) = 0.54$$

These numbers are at least better than the state of the art, in the systematic error studies for the luminosity sharing, of $p_{e^+} = 30\%$, [6].

Appendix

Consider the decay of a generic Higgs H going to Z and Gamma, with a coupling noted by g .

The only leading CP violating that are $Z_\mu H A^\mu$ and $Z_\mu H^3 A^\mu$.

Write 1st $Z_\mu H A^\mu$ Ward identity for v_1 then for v_2 ,

$$\begin{aligned} & \int_0^\Lambda d^4 k' \frac{\epsilon_\mu(k)}{(k+k')^2} \frac{1}{k'^2} \frac{\epsilon^\mu(q_Z)}{(q_Z - k')^2 + M_Z^2} \\ &= \int_0^\Lambda \int_0^\Lambda d^4 q'_Z d^4 k' \frac{1}{(q'_Z + q_Z)^2 + M_Z^2} \frac{\epsilon_\mu(k)}{k'^2} \frac{\epsilon^\mu(q_Z)}{(q_Z - k')^2 + M_Z^2} \\ &- \int_0^\Lambda \int_0^k d^4 k'' d^4 k' \frac{1}{(k'' + k')^2} \frac{\epsilon_\mu(k)}{(k'' + k')^2} \frac{\epsilon^\mu(q_Z)}{k'^2} \end{aligned}$$

For, $Z_\mu H^3 A^\mu$ one uses the external-internal separation i.e. that of $H^3 = H^{(\text{ext})} H^{2(\text{int})}$.

With the Goldstone breaking applied into the internal, so one simply gets the previous tree diagram plus the tree diagram with a blob on it.

These equations are true only for a single Higgs. Which is not true for our case since there are, neglecting in the lower energy domain the Heavy Higgs Pseudo-scalars, H_1 and H_2 which have a certain mixing plus different vacuum decay's values.

H_1, H_2

$$H_1 H_1 H_1, H_1 H_2 H_1 + 2 \leftrightarrow 1, H_1 H_2 H_2$$

$$H_2 H_1 H_1, H_2 H_2 H_1 + 2 \leftrightarrow 1, H_2 H_2 H_2$$

Giving then the values, defining $g_i \equiv g_i^{\text{HZA}}$

$$g_1, g_2$$

$$\lambda_{111} \times v_1^2, 2\lambda_{121} \times v_1 \times v_2, \lambda_{122} \times v_2^2$$

$$\lambda_{211} \times v_1^2, 2\lambda_{221} \times v_1 \times v_2, \lambda_{222} \times v_2^2$$

Adding altogether,

$$g_1 + g_2 + (\lambda_{111} + \lambda_{211})v_1^2 + 2(\lambda_{121} + \lambda_{221})v_1 \times v_2 + (\lambda_{122} + \lambda_{222})v_2^2$$

As there is mostly true approximation, $\frac{g_2}{g_1} \cong \frac{\lambda_2}{\lambda_1}$, for various λ 's, so

$$g_1 \times (1 + a) + \lambda_{111} \times (1 + a)v_1^2 + 2\lambda_{121} \times (1 + a)v_1 \times v_2 + \lambda_{122} \times (1 + a)v_2^2$$

These formulas apply, being submitted to the spontaneously breaking, to the RHS case.

Which brings their equation to the following form

$$\begin{aligned} & g_1 \int_{m_{s0}}^{\Lambda(0)} d^4 k' \frac{\epsilon_\mu(k)}{(k+k')^2} \frac{1}{k'^2} \frac{\epsilon^\mu(q_Z)}{(q_Z-k')^2 + M_Z^2} + g_2 \int_{m_s}^{\Lambda(m_s)} d^4 k' \frac{\epsilon_\mu(k)}{(k+k')^2} \frac{1}{k'^2} \frac{\epsilon^\mu(q_Z)}{(q_Z-k')^2 + M_Z^2} \\ & + (\lambda_{111} + \lambda_{211})v_1^2 \int_{m_{s0}}^{\Lambda(0)} d^4 k' \frac{\epsilon_\mu(k)}{(k+k')^2} \frac{1}{k'^2} \frac{\epsilon^\mu(q_Z)}{(q_Z-k')^2 + M_Z^2} \\ & + 2(\lambda_{121} + \lambda_{221})v_1 \times v_2 \int_{m_s}^{\Lambda(m_s)} d^4 k' \frac{\epsilon_\mu(k)}{(k+k')^2} \frac{1}{k'^2} \frac{\epsilon^\mu(q_Z)}{(q_Z-k')^2 + M_Z^2} \\ & + (\lambda_{122} + \lambda_{222})v_2^2 \int_{2m_s}^{\Lambda(2m_s)} d^4 k' \frac{\epsilon_\mu(k)}{(k+k')^2} \frac{1}{k'^2} \frac{\epsilon^\mu(q_Z)}{(q_Z-k')^2 + M_Z^2} \end{aligned}$$

Integrations with $\int_{m_{s0}}^{\Lambda(0)}$ eliminate, while noting $dk'D = d^4 k' \frac{\epsilon_\mu(k)}{(k+k')^2} \frac{1}{k'^2} \frac{\epsilon^\mu(q_Z)}{(q_Z-k')^2 + M_Z^2}$, so

$$\begin{aligned} & [g_2 + 2(\lambda_{121} + \lambda_{221})v_1 v_2] \left[\int_{m_s}^{\Lambda(m_s)} dkD - \int_{m_{s0}}^{\Lambda(0)} dkD \right] \\ & + (\lambda_{122} + \lambda_{222})v_2^2 \left[\int_{2m_s}^{\Lambda(2m_s)} dkD - \int_{m_{s0}}^{\Lambda(0)} dkD \right] \end{aligned}$$

View $\int_{m_{s0}}^{\Lambda(0)} D = \int_{m_{s0}}^{m_s} D + \int_{m_s}^{\Lambda(m_s)} D - \int_{\Lambda(0)}^{\Lambda(m_s)} D \Rightarrow \int_{m_s}^{\Lambda(m_s)} D - \int_{m_{s0}}^{\Lambda(0)} D = -\int_{m_{s0}}^{m_s} D + \int_{\Lambda(0)}^{\Lambda(m_s)} D$, which can

be written due the large values of Λ compared to the integration parameters as

$$-\int_{m_{s_0}}^{m_s} D(k) + [\Lambda(m_s) - \Lambda(0)] \times D(\Lambda(0)) = -\int_{m_{s_0}}^{m_s} D(k) + m_s \Lambda'(m_s) \times D(\Lambda(0))$$

Since, $m_s \geq m_{s_0}$ is not zero in value and can reach up to being close to m_Z , one can work the integrations exactly and after a trivial collection of terms by adding the missing integration domains, all the RHS eliminates while from the LHS there remains

$$(g_2 + 2(\lambda_{121} + \lambda_{221})v_1) \int_0^{m_s} d^4k' \frac{\epsilon_\mu(k)}{(k+k')^2} \frac{1}{k'^2} \frac{\epsilon^\mu(q_Z)}{(q_Z-k')^2 + M_Z^2} =$$

$$-(\lambda_{122} + \lambda_{222})v_2 \int_0^{2m_s} d^4k' \frac{\epsilon_\mu(k)}{(k+k')^2} \frac{1}{k'^2} \frac{\epsilon^\mu(q_Z)}{(q_Z-k')^2 + M_Z^2}$$

So defining $\int_a^\Lambda d^4k' \frac{\epsilon_\mu(k)}{(k+k')^2} \frac{1}{k'^2} \frac{\epsilon^\mu(q_Z)}{(q_Z-k')^2 + M_Z^2} = F(a)$, the equation can be written as

$$(g_2 + 2(\lambda_{121} + \lambda_{221})v_1) = -2(\lambda_{122} + \lambda_{222})v_2$$

As v_2 relates to v_1 and the lambda relates to the Yukawa's it can be deduced the above used form.

References

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