

# Review of: "Integer topological proof of Dirichlet's theorem"

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Potential competing interests: No potential competing interests to declare.

Dirichlet's theorem on primes in arithmetic progressions is an important result, and a purely topological proof of this fact would be very interesting and surprising. Unfortunately though, I was not able to follow the argument in this paper. Some places where I became confused:

1. If I understand correctly, you are considering a topology on the set of all integers, rather than on the set of positive integers (which is where Golumb's original topology was defined). If 0 is an element of a set  $S(p,q)$  with  $(p,q) = 1$ , then  $p$  must divide  $q$ , hence  $p = \pm 1$ , and therefore  $S(p,q) = \mathbb{Z}$ . This implies that the singleton  $\{0\}$  is dense, which seems to contradict Lemma 2.0.0.1(1).
2. I could not understand the statement of Theorem 2.0.1. In the statement,  $p$  and  $q$  are fixed, correct? What is  $n$ ? Is the theorem stating that there is some  $n$  for which the closure of  $S^*(s(n),n)$  is contained in  $\mathbb{Z} \setminus s_p$ ?