

Research Article

Development of Body Fat Estimation Equations Based on BMI, Age, Gender, and Ethnic Groups

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Body fat (BF) percentage is a measurement of human health. The simple predictive equation between BF and the anthropometric measurement helps evaluate the BF value. The BMI value, weight divided by the height square, has been used as the significant factor in BF values. However, other factors involving age, gender, and ethnicity may also affect the BF values. An adequate model considering all influencing factors is critical in predicting the BF value. Many empirical equations have been proposed to evaluate these factors. This study uses previously collected data to establish the BF equation with modern regression analysis. Three forms of body mass index (BMI), BMI, logarithmic BMI, and inverse BMI, are selected as independent variables. The other variables include age, gender, and ethnicity. The t-value was used to test the significant influence of each variable in the regression equations. The Prediction Sum of Squares (PRESS) statistics were used to evaluate the models' predictive ability. Categorical testing was adopted to evaluate the significant influence of these variables of age, gender, and ethnicity. The results of this study indicated that the best BF model involved BMI, BMI², age, and age² variables. The age, gender and ethnicity tested by categorical test significantly affected BF values. No single form of the BF equation can be proposed to represent all ethnicities or both genders. Modern regression analysis can provide more scientifically based model-building techniques than machine learning. By calculating the BMI value, the cutoff point of BF values needs to consider the difference between gender and ethnicity. The regression technique in this study provides a reasonable method to establish the BF equation for different ethnicities and other factors.

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1. Introduction

Body fat percentage (BF) is an essential measurement of human health. It also affects the pharmacokinetics of most drugs^[1]. The fat fraction significantly affects the human propofol kinetics^[2]. The BF values could be measured directly by using bioimpedance spectroscopy (BIS), bioelectrical impedance analysis (BIA), air displacement plethysmography, and electrical impedance myography (BIM). However, these measurement methods are expensive and time-consuming. Body mass index (BMI) is calculated by a subject's weight and height and is then used to predict the BF value. It provides a simple way to find the BF values. Overweight or obesity is a risk factor for chronic disease. The cut-off points for overweight or obesity are generally defined as a certain BMI threshold value^{[3][4]}.

Some empirical models have been proposed to describe the relationship between BF and other influencing factors. Due to its simplicity, BMI serves as the standard variable to predicate BF and is then used to classify the degree of obesity. However, some evidence suggests the BMI cut-points may not be the same for all ethnic groups^[5]. The relationship between fat and BMI in gender and different ethnic groups may provide an explanation.

Some researchers reported the change in fat at a given BMI is affected by age and gender^{[6][7]}. The relationship between BF and BMI and other influencing factors needs to be further studied and validated.

Researchers have introduced different empirical equations. Deurenberg et al.^[7] proposed two linear equations representing the effect factors on BF. The coefficient of determination, R^2 , and estimated value of standard errors of these models were used to evaluate the adequacy of the proposal model. The ethnicity of the subjects was not mentioned. Gallagher et al.^[8] introduced the linear equation to express the relationship between BF and BMI. Age and gender did not significantly influence BF. However, Deurenberg et al.^[9] proposed the predictive equation: $BF = b_0 + b_1BMI + b_2age + b_3gender$. The effect of ethnicity on the BF values was observed by the calculated values at fixed BMI values in subjects of different ethnicities, with the effects found to be inconsistent.

Gallagher et al.^[10] introduced a complex multiple-linear equation to predict BF values. The independent variables included the inverse function of BMI (BMI^{-1}), sex, age, ethnicity, and the interaction of variables. Jackson et al.^[11] studied the relationship between BF and BMI for subjects

including race (white and black) and gender (men and women). The polynomial equation was established as $BF = c_0 + c_1BMI + c_2BMI^2$. Age, ethnicity, and ethnicity and BMI interaction were found to have no significant effect on the BF value.

To establish the obesity cutoffs for Taiwanese subjects, Chang et al.^[12] proposed a linear regression model as $BF = d_0 + d_1BMI$, and the new BMI cutoffs of overweight and obesity were suggested for male and female Taiwanese adults. Kagawa et al.^[13] performed a study to evaluate the relationship between BF and BMI for young Japanese and Australian men. Both independent and dependent variables were in logarithmical form, $LnBF = e_0 + e_1Ethnicity + e_2LnBMI$. Ethnicity significantly affected the relationship between $LnBMI$ and $LnBF$. Larson et al.^[14] measured BF and other anthropometric variables to assess the effect variables on the BF values. Two indexes, weight/height (W/H) and weight/(height)², were compared for the predictive performance. Their result indicated that the W/H value may be a more valuable index than that of W/H² (BMI) in expressing the effect on BF, especially at higher body weights. However, the criteria to evaluate the performance of these models were the correlation coefficient and absolute errors. Rush et al.^[15] compared the difference between BMI and BF values in women of five ethnicities from two countries. The proposed equation was $BF = f_0 + f_1LogBMI$. The R² and s were the criteria to evaluate these data. Their results indicated no single form of the BF equation and BMI cut-points could be established. Meeuwssen et al.^[16] observed UK adults and proposed a curvilinear mode to express the influence factors on BF. Gomez-Ambrosi et al.^[17] recommend a BF prediction equation with more variables and interaction of variables, such as age, gender, BMI, BMI², BMI*gender, BMI*age, BMI²*gender, BMI²*age.

The model developed by Gomez-Ambrosi et al.^[17] was adopted by Fuster-Parra et al.^[18]. The fitting agreements of the BF model with BMI and the body adiposity index (BAI) were compared, and it was found that the BAI variable had better predictive ability than that of BMI. The correlation coefficient served as the criterion for comparing.

Cortes-Castell et al.^[19] developed a new model to predict the BF values of children in Spain. Itani et al.^[20] proposed the BF models for the men and women of Lebanese. The variables included BMI², 1/BMI, and age. In research on body fat prediction models in American adults^[21], more anthropometric measurements, such as waist circumference, hand thickness, vertical abdominal skinfold, and thigh skinfold, were incorporated into the BF model.

To consider obesity as a public health problem, the BF prediction model was developed in different countries, such as Mexico^[22], Vietnam^[23], Nigeria^[24], Serbia^[25], Saudi Arabia^[26], Italy^[27], Philippines^[28], and Lebanon^[20].

The published models using data involving several variables are listed in Table 1.

Reference	Regression equations	BMI range	
1. Womersley and Durnin ^[7]	1a. Men $BF = -12.47 + 1.34BMI$ 1b. Women $BF = -3.47 + 1.37BMI$		
2. Deurenberg et al. ^[6]	2a. Children (ages ≤ 15) $BF = 1.4 + 1.51BMI - 0.70age - 3.6gender$, $R^2 = 0.38$, $s = 0.044$ 2b. Adults $BF = -5.4 + 1.20BMI + 0.23age - 10.8gender$, $R^2 = 0.79$, $s = 0.041$	16–36.5	
3. Gallagher et al. ^[8]	3a. Black, Women $BF = -6.254 + 1.419BMI + 0.07age$, $R^2 = 0.58$ 3b. White, Women $BF = -11.666 + 0.1591BMI + 0.096age$, $R^2 = 0.56$ 3c. Black, Men $BF = -18.624 + 1.367BMI + 0.105age$, $R^2 = 0.44$ 3d. White, Men $BF = -22.519 + 1.402BMI + 0.177age$, $R^2 = 0.52$		
4. Deurenberg et al. ^[9]	Caucasian $BF = -8.0 + 1.294BMI + 0.20Age - 11.4gender$, $R^2 = 0.88$	19–31	
5. Gallagher et al. ^[10]	White and African American $BF = 84.8/BMI + 0.079age + 16.4gender + 0.05Sgender*age + 39.0gender/BMI$, $R^2 = 0.86$	16–38	
6. Jackson et al. ^[11]	6a. Female $BF = -82.83 + 34.43\ln BMI + 0.14age - 26.02gender - 7.48gender*BMI$, $R^2 = 0.82$, 6b. Male $BF = -149.24 + 51.31\ln BMI + 1.47age - 0.41age*\ln BMI$, $R^2 = 0.82$ 6c. Heritage Woman $BF = -46.24 + 4.35BMI - 0.05BMI^2$, $R^2 = 0.78$ 6d. Heritage Man $BF = -47.8 + 3.76BMI - 0.04BMI^2$, $R^2 = 0.68$	17–47	
7. Chang et al. ^[12]	Taiwan 7a. Women $BF = -3.07 + 1.652BMI$, $R^2 = 0.6$	14–33 15–33	

Reference	Regression equations	BMI range	
	7b. Men $BF = -9.093 + 1.38BMI$, $R^2 = 0.475$		
8. Kagawa et al. [13]	Japanese and Australian Caucasian $\ln BF = -3.321 - 0.123 \text{ Ethnicity} + 1.941 \ln BMI$, $R^2 = 0.548$, $s = 0.21$	15.6~36.6	
9. Larson et al. [14]	Swedish 9a. Women $BF = -28.27 + 1.895BMI$, $R^2 = 0.61$ 9b. Man $BF = -49.47 + 3.865 BMI - 0.0343 BMI^2$, $R^2 = 0.72$	17~46	
10. Rush et al. [15]	Women, five ethnicities, two countries 10a. SA, European $BF = -83.6 + 82.9 \text{ LogBMI}$, $R^2 = 0.73$, $s = 4.9$ 10b. NZ, European $BF = -111.2 + 105.2 \text{ LogBMI}$, $R^2 = 0.80$, $s = 4.8$	16.1~48.0	
11. Levitt et al. [29]	Caucasian, Hispanic, Black 11a. Women $BF = 64.2 - 9.23/BMI + 0.132age$ 11b. Men $BF = -20.6 + 1.27BMI + 0.182age$	17.07~65.75	
12. Meeuwse et al. [16]	UK adults $BF = -32.515 + 12.409gender + 3.306BMI - 0.030BMI^2 - 0.006age$ $+ 0.033age*gender - 0.001age*BMI$,	14.5~45.5	
13. Gomez-Ambrosi et al. [17]	Caucasian, Spain adult $BF = -44.988 + 0.503age + 10.689gender + 3.172 BMI - 0.026BMI^2$ $+ 0.181 \bullet BMI*gender - 0.02BMI*Age - 0.005BMI^2*gender$ $+ 0.0021 BMI^2*age$, $R^2 = 0.774$, $s = 4.7$	13.8~70.2	
14. Fuster-Parra et al. [18]	Caucasian, Spain adults $BF = -44.988 + 0.503age + 10.689 gender + 3.172BMI - 0.026BMI^2$ $+ 0.181BMI*gender - 0.02 \bullet BMI*Age - 0.005BMI^2*gender$ $+ 0.00021 \bullet BMI^2*Age$, $R^2 = 0.79$	15.8~51.3	

Reference	Regression equations	BMI range	
15. Ho-Pham et al. ^[23]	Vietnamese BF=18.9-10.9gender+0.044age +3.472BMI-0.05BMI ² R ² =0.71, s=3.90	15-36	
16. Akindele et al. ^[24]	Nigeria BF=0.583BMI+0.456gender+0.152age, R ² =0.82	10-58	
17. Jelena et al. ^[25]	Serbian, adults BF=-5.4+0.23age-10.8gender+1.2BMI	16.8-33	
18. Eldeen et al. ^[26]	Saudi Arabian, adults BF=-5.4+0.23age-10.8gender+1.20BMI	15-30.5	
19. Cortes-Castell et al. ^[19]	Spain children 19a. Boy BF= 18.655+0.007BMI ² -293.601/BMI+0.112age-0.018age ² 19b. Girls BF=18.655+0.007BMI ² -293.601/BMI	18.6-34.6	
20. Itani et al. ^[20]	Lebanese, adults 20a. Women BF= 21.835+0.622BMI, R ² =0.718 s=3.81 20b. Men BF=-4.001+1.050 BMI, R ² =0.709 s=3.88	24-55	
21. Molina-luque et al. ^[21]	Spain, adults BF=-97.102+0.123age-11.9gender+35.959BMI	21.5-30.8	
22. Chen et al. ^[30]	Singaporean, adults 19a. Men BF= 49.818+00.089age-610.808/BMI 19b. Women BF=58.159+0.051age-516.401/BMI	15.1-39.9	
23. Kalaragunta et al. ^[31]	India, adults 20a. Women BF= -5.4+0.23age-10.8gender+1.2BMI	18.5-29.9	

Table 1. Published models and Statistical tests of the body mass index (BMI) and body BF.

Note: BF: percentage body fat in %, BMI: body mass index in Kg/m², age in years, gender: men and women, categorical variables.

Recently, researchers have examined the predictive performance of different BF models. Nickerson et al.^[32] evaluated the relative accuracy of Womersley and Durnin^[6], Jackson et al.^[11], Deurenberg et al.^[7] and Gallagher et al.^[10]. Inconsistent results were found in subjects of both men and women. Jaafar et al.^[33] assessed the accuracy of the BF estimation in Arab people with the above four models and the Gomez-Ambrosi model^[17]. The equation of Jackson et al.^[11] was recommended as the best model for obesity in the Lebanese population. De Nortoli et al.^[34] recommended that the Gomez-Ambrosi equation be better than other BMI equations for patients undergoing bariatric surgery.

In the above introduction, most studies use R² as the sole criterion. Some studies select s and the p-value to evaluate the validations of a BF model. However, these criteria (R², s, and p-value) are only used for classical regression^{[35][36]}.

Besides the regression methods, Faradisa et al.^[37] used fuzzy logic to establish the relationship between BF and BMI. The fuzzy sets of body weight, height, and BMI were 3, 3, and 5, respectively. They found that the BF and BMI can produce the same categories. Xu et al.^[38] adopted a supervised machine-learning approach to develop the prediction equation for BF and BMI. Gender, income, age, and education were the affecting factors. Their best model included 18 variables and 19 parameters.

This study adopts a modern regression technique to evaluate the adequateness of different BF models and determine the factors affecting the BF values. Modern regression techniques, such as residual plots, the normal test, the constant variance test, the test on a single regression coefficient, and categorical testing, are used in this study to develop the BF models. The statistics, Prediction Sum of Squares (PRESS) is used to assess the prediction ability of the models^{[28][32]}. A modern regression technique was applied in liver volume prediction^[33], plant tissue culture^[34], water activity in floral honey^[35], and dielectric properties of foods^[36].

To the best of the authors' knowledge, the modern regression technique has not been adopted in the study of BF models. Here, the adequateness of BF models was evaluated, and the factors affecting the Bf values of different subjects were determined using data from previous studies.

2. Materials and Methods

2.1. Regression analysis

In this study, the dependent variable y_i is the BF. The independent variables include BMI, age, gender, and ethnicity. The BMI and age are continuous variables, and gender and ethnicity are categorical variables.

The effect of BMI and age on BF is evaluated with a typical multiple regression model:

$$BF = b_0 + b_1BMI + b_{11}BMI^2 + b_2age + b_{22}age^2 + b_{12}BMI*age \quad (1)$$

where $b_0, b_1, b_{11}, b_2, b_{22}, b_{12}$ are constants.

This equation is called the BMI equation.

The diagnostic techniques of modern regression analysis are described as follows:

2.1.1. Normality test

The Kolmogorov-Smirnov test verifies the normal data distribution. The p-value determines its probability.

2.1.2. Residual Plots

For the residual plot, the residuals are on the longitudinal axis, and the predicted value of the model is on the horizontal axis. If the uniform distribution of errors along the $y_i=0$ line is presented, the regression model is adequate. If the fixed pattern of the data distribution is found, the model is not suitable. The funnel pattern indicates that the error variance is not constant; that is, it is a heterogeneous variance.

2.1.3. Transformation

Two forms of transformation are used in this study. Previous research has recommended this transformation^{[4][13][19]}. Two equations are proposed for further study:

$$BF = c_0 + c_1\ln BMI + c_{11}(\ln BMI)^2 + c_2age + c_{22}age^2 + c_{12}(\ln BMI)*age \quad (2)$$

where $c_0, c_1, c_{11}, c_2, c_{22}$ and c_{12} are constants.

The equation is called the logarithmic BMI equation.

$$BF = d_0 + d_1(1/BMI) + d_{11}(1/BMI)^2 + d_2age + d_{22}age^2 + d_{12}(1/BMI) * age \quad (3)$$

where d_0 , d_1 , d_{11} , d_2 , d_{22} and d_{12} are constants.

The equation is called the inverse BMI equation or 1/BMI equation.

2.2. Categorical testing

Influencing factors, such as gender and ethnicity, are categorical variables. The categorical test technique is used to determine their significance.

2.2.1. Two categories.

The two categories of gender (men, women) and ethnicity (Black, Mexican) can be tested for their level of effect on the BF values. The BF equation linking the dependent variable and two variables is:

$$BF = b_0 + b_1BMI + b_{11}BMI^2 + b_2age + b_{22}age^2 + b_{12}BMI * age \quad (4)$$

Let Z be defined as follows:

$Z=0$, if in the male category

$Z=1$, if in the female category

The equation to determine the significant effect of the two levels as a factor is:

$$BF = e_0 + e_3Z + e_1BMI + e_{13}BMI * Z + e_{11}BMI^2 + e_{113}BMI^2 * Z + e_2age + e_{23}age * Z + e_{22}age^2 + e_{23}age^2 * Z + e_{12}BMI * age + e_{123}BMI * age * Z + \varepsilon_i \quad (5)$$

where all e_{ii} are constants, and Z is the categorical value. The significant effect of this factor can be determined by testing these e_i or e_{ii} values.

2.2.2. Multiple categories

More categories can be considered, such as three ethnicities and gender. The Z_i can be defined as Table 2.

Ethnicities	Gender	Z1	Z2	Z3
A	men	0	0	0
A	women	0	0	1
B	men	1	0	0
B	women	1	0	1
C	men	0	1	0
C	women	0	1	1

Table 2. Example of multiple categories.

The equation to determine the significance of ethnicity and gender is:

$$\begin{aligned}
 BF = & b_0 + f_1 Z_1 + f_2 Z_2 + f_3 Z_3 + b_1 BMI + g_1 Z_1 BMI + g_2 Z_2 BMI + g_3 Z_3 BMI \\
 & + b_{11} BMI^2 + f_{11} Z_1 BMI^2 + f_{22} Z_2 BMI^2 + f_{33} Z_3 BMI^2 + C_1 age + g_1 Z_1 age \\
 & + h_2 Z_2 age + h_3 Z_3 age + c_{11} age^2 + h_{11} Z_1 age^2 + h_{22} Z_2 age^2 + h_{33} Z_3 age^2 \\
 & + C_{12} age * BMI + k_1 Z_1 age * BMI + k_2 Z_2 age * BMI + k_3 Z_3 age * BMI \quad (6)
 \end{aligned}$$

2.3. Statistical analysis

This statistical analysis uses sigma plot V.14.0 (SPSS Ing., Chicago, IL, USA). To evaluate a variable's significance, the t-value of its parameter is tested. The hypothesis is.

$$H_0: b_i = 0$$

$$H_1: b_i \neq 0$$

The t-value of b_i is:

$$t = \frac{b_i}{se(b_i)} \quad (7)$$

where b_i is the variable's parameter value and $se(b_i)$ is the standard error of b_i . The coefficient of determination, R^2 , and the estimation value of standard errors, s , are used as criteria to compare the models' fitting agreement.

The Variance Inflation Factor (VIF) is a statistic that detects the multicollinearity between these independent variables.

2.4. The PRESS statistics

The statistics PRESS is used to evaluate the models' predictive ability^[35].

A statistic, the prediction sum of squares (PRESS), is adopted to evaluate the regression model's prediction ability. Considering a data set of size n , PRESS is calculated by omitting each observation individually. Then, the remaining $n - 1$ observations are used to estimate the coefficients for a candidate model. This regression equation is used to predict the value of the omitted response value (denoted by $\hat{y}_{-i}$). We then calculate the i th PRESS residual as the difference $y_i - \hat{y}_{-i}$. Then, the calculation for PRESS is given by $PRESS = \sum (y_i - \hat{y}_{-i})^2$. The observation y_i was not used for fit and assessment, so the i th PRESS residual could serve as a criterion for evaluating prediction ability.

The smaller the PRESS value, the better the model's predictive ability

2.5. BF data source

The data of this study are provided by Dr. Steven B. Heymsfield^[39]. All data are from NHANES (National Health and Nutrition Examination Survey) 1999–2006. There are eight data sets in this study. The four ethnicities are White, Black, Mexican, and others. The other group includes Asians, Puerto Ricans, and other countries. However, the number of others is limited. Each ethnicity has two sub-sets of data: men and women. The descriptive statistics of the subjects in different groups are listed in Table 3. The BF was measured using the dual-energy X-ray absorptiometry (DXA) technique.

3. Results

3.1. Descriptive statistics

Table 3 shows the general and anthropometric characteristics of the sample. For the four ethnicities, women had higher mean BF values than men. Mexican women had the highest mean BF values of the other three ethnicities. Similar results were found for the mean BF values.

Sample & variables	Black men	Black women	White man	White women
No. of Subjects	2,286	2,284	2,320	2,366
Age (years)	29.54±20.48	32.53±20.84	43.26±24.13	44.52±23.04
Weight(kg)	73.75±26.25	73.64±24.38	79.50±22.58	70.11±19.06
Stature(cm)	169.80±14.20	160.41±9.23	172.75±12.32	161.58±8.03
BMI(kg/m ²)	24.97±6.88	28.25±8.34	26.21±35.08	26.70±6.66
Waist circumference (cm)	85.26±19.56	90.25±19.45	94.77±17.74	90.55±16.22
BF (%)	24.26±7.85	37.16±8.25	27.85±6.74	38.61±7.44
BF mass(g)	19.26±12.32	29.01±15.08	23.17±10.83	38.16±13.30
Lean soft tissue(g)	52.81±15.88	42.52±10.08	54.48±13.25	40.02±7.74
Total mass(g)	74.80±26.76	73.66±24.59	80.13±22.80	70.15±19.32
	Mexican men	Mexican women	Others men	Others women
No. of Subjects	2,218	2,258	1,043	938
Age(years)	28.39±19.91	33.15±20.85	31.96±20.20	34.22±19.98
Weight(kg)	68.8±20.23	65.69±18.80	71.58±22.04	64.77±19.08
Stature(cm)	163.47±13.22	155.58±8.53	166.89±13.21	156.98±9.01
BMI(kg/m ²)	25.20±6.04	26.91±6.78	25.09±5.74	26.01±6.55
Waist circumference (cm)	88.10±17.40	89.53±16.30	88.14±16.88	87.49±16.20
BF (%)	28.13±7.8	38.87±6.93	26.57±6.94	37.37±7.16
BF mass(g)	20.32±10.54	24.46±11.48	19.81±9.76	24.97±11.49
Lean soft tissue(g)	47.27±13.23	37.24±8.09	45.54±13.72	37.34±8.30
Total mass(g)	69.71±22.45	65.54±18.97	72.03±22.18	64.18±19.90

Table 3. Descriptive statistics of subjects in different ethnic groups.

3.2. Evaluate the adequate BF equations.

3.2.1. Black men

The relationship between BF and BMI for black men is presented in Figure 1. The BMI and age are assumed as the factors of the BF value.

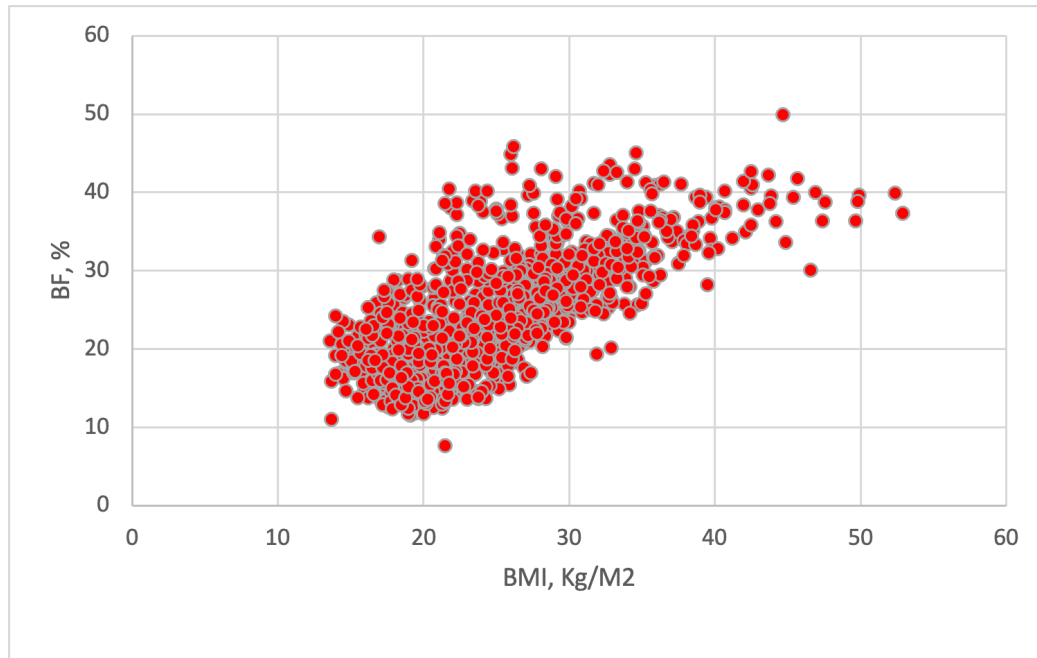


Figure 1. Relationship between BF and BMI for black men.

The results of the multiple regression are as follows:

The members in parentheses below the estimated values of the parameters are the t values for these estimated values.

$$BF = -0.38 + 1.708BMI - 0.0126BMI^2 - 0.684age + 0.00851age^2 + 0.0000323BMI \cdot age$$
$$(-0.171) (12.301) (-5.47) (-14.29) (17.15) (0.0241) (8)$$

The t-value for BMI•age was 0.0241. Thus, the term BMI•age had no significant effect on the BF equation.

The adequate equation was as follows:

$$BF = -0.314 + 1.698BMI - 0.0125BMI^2 - 0.685age + 0.00842age^2$$
$$(-0.176) (12.320) (-5.328) (-17.792) (14.393)$$

$R^2=0.791$, $s=4.675$, $PRESS=50,176$ (9)

The Kolmogorov-Smirnov test indicated the data distribution of BF was normal. The residual plots of equation (9) are shown in Figure 2a. The uniform distribution of the residuals indicated constant variance.

For the logarithmic BMI value, BMI served as the dependent variable, and the results of the regression analysis are as follows:

$$BF = 37.375 - 28.211 \ln BMI + 8.383 (\ln BMI)^2 - 0.662 \text{age} + 0.00821 \text{age}^2 \quad (10)$$

$R^2=0.613$, $s=4.691$, $PRESS=50,555$

The normal test of this equation failed. Figure 2 b shows the residual plot of the BF vs $\ln BMI$ equation. The fixed pattern of this residual distribution indicates that the variance of this model is not constant.

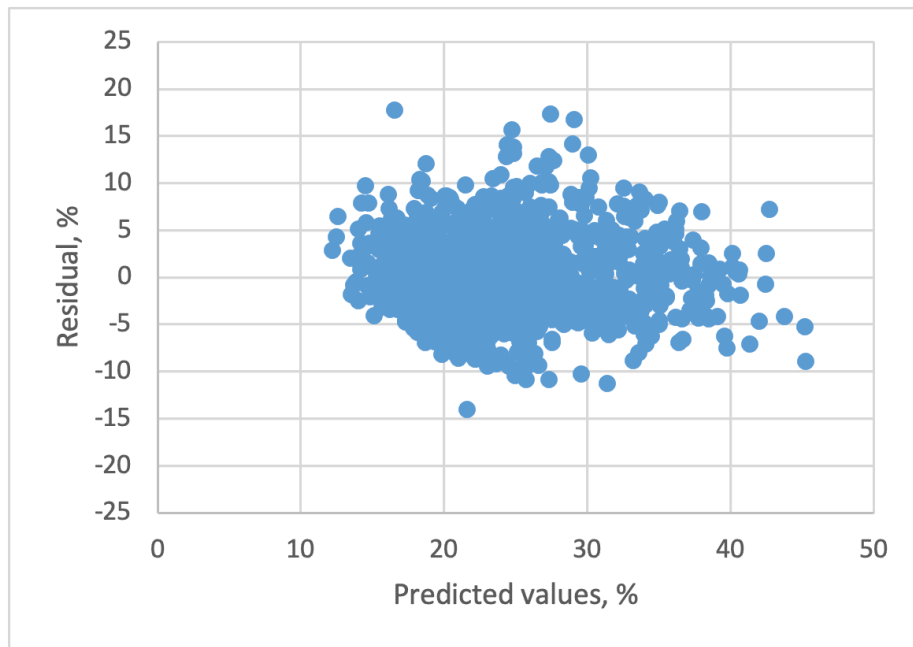
When comparing the BF vs. BMI equation, the model had larger s and $PRESS$ values and smaller R^2 values. That is, the fitting agreement and predictive ability were not better than those of the previous BMI model.

As the inverse BMI served as the new variable, the results of regression analysis are as follows:

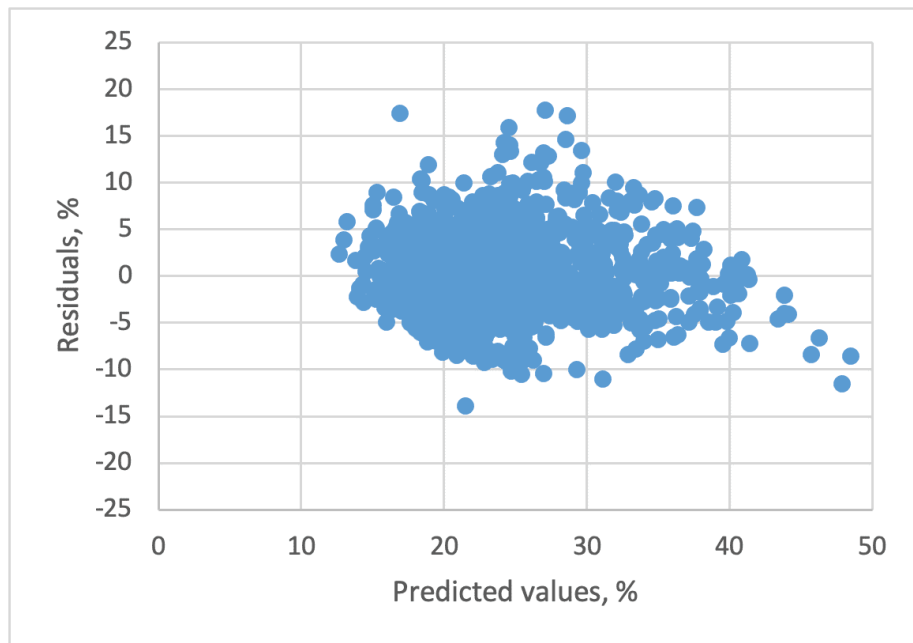
$$BF = 85.430 - 1869.322 (1/BMI) + 14321.597 ((1/BMI)^2 - 0.653 \text{age} + 0.00805 \text{age}^2) \quad (11)$$

$R^2=0.637$, $s=4.605$, $PRESS=49,686$

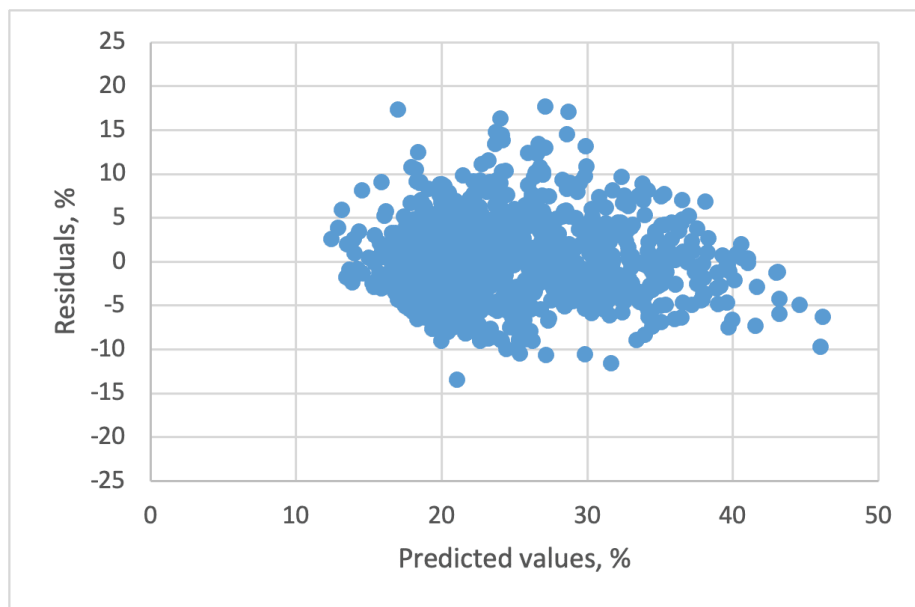
The residual plot of the BF vs. $1/BMI$ equation is shown in Figure 2c. A fixed pattern could be found, but the variance was not uniform. The normal test failed. At the higher predicted values, the errors were positive. This is a typical overestimation error. Comparing these three equations, the $1/BMI$ equation had the smallest values of s and $PRESS$ and the most considerable R^2 value. The quantitative criteria of the fitting agreement and perceived performance were close between the BMI and $1/BMI$ equation. However, only the BMI equation could pass the normal test and homogenous variance tests. It was recognized as an adequate model.



(a). BMI equation



(b). Ln(BMI) equation



(c). 1/BMI equation

Figure 2. Residual plots of the BF equation for black men.

3.2.2. Black women

The data distribution between BF and BMI for black women is shown in Figure 3.

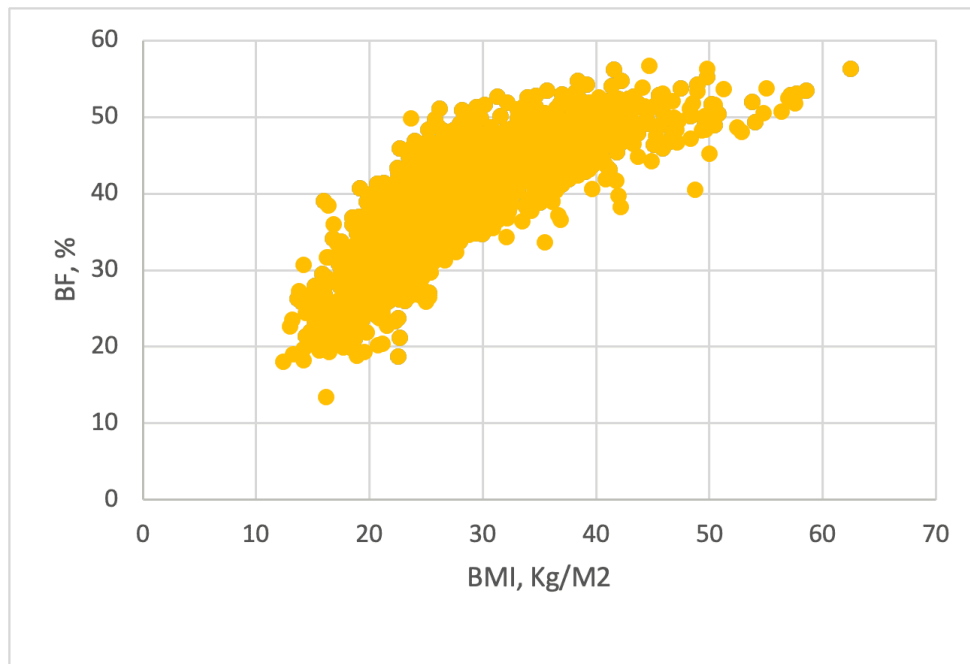


Figure 3. Relationship between BF and BMI for black women.

The regression analysis of BF and its influencing factors are as follows:

$$BF = -4.371 + 2.0878BMI - 0.0206BMI^2 + 0.0364age + 0.000439age^2 - 0.0000245BMI*age$$

$$(-4.201) (30.858) (-19.462) (1.622) (2.313) (-0.434) (12)$$

The t-value of the estimated value of BMI*age was -0.434. It did not have a significant effect on the BF. The adequate model is:

$$BF = -4.207 + 2.083BMI - 0.0207BMI^2 + 0.0306age + 0.000432age^2$$

$$(-4.348) (31.164) (-19.922) (1.698) (12.285)$$

$$R^2=0.769, s=3.697, PRESS=31,944 (13)$$

The normal test passed. The residual plots are shown in Figure 4a. The uniform distribution revealed the constant variance.

By transforming the logarithmic BMI value, the lnBMI equation is:

$$BF = -115.846 - 69.069\ln BMI - 6.843(\ln BMI)^2 + 0.0159age + 0.00564age^2 (14)$$

$$R^2=0.767, s=3.708, PRESS=32,362$$

The equation passed the normal test. The residual plots are shown in Figure 4b. A fixed pattern was found. As the predicted value was below 25%, all residuals were positive and showed over-estimation

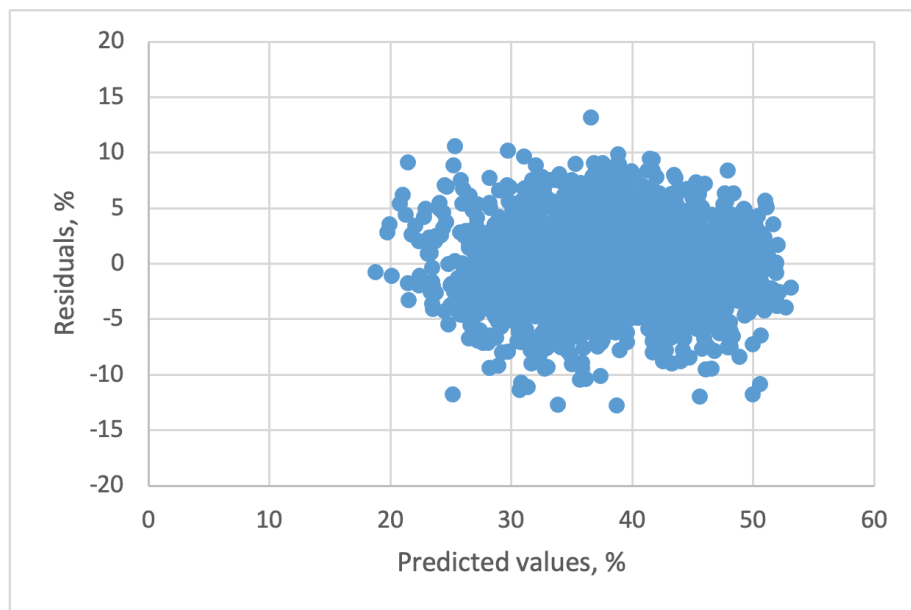
trending. This equation could not be recognized as an adequate model.

The transform form of $1/\text{BMI}$ was used as an independent variable. The regression equation is as follows:

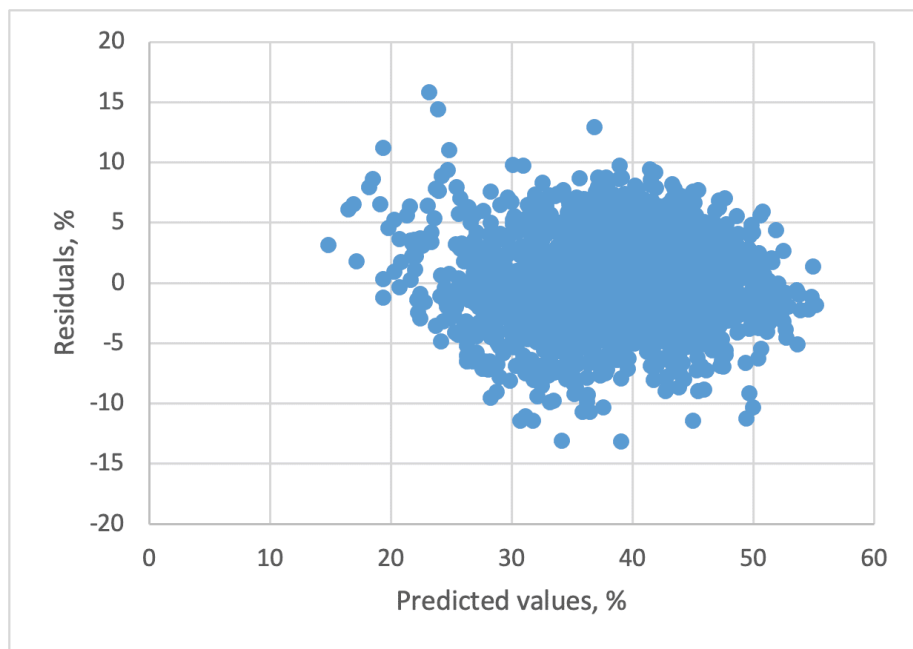
$$\text{BF} = -68.128 - 1011.3 (1/\text{BMI}) + 4742.125((1/\text{BMI})^2 + 0.0232\text{age} + 0.000504\text{age}^2) \quad (15)$$

$$R^2=0.769, s=3.697, \text{PRESS}=31,843$$

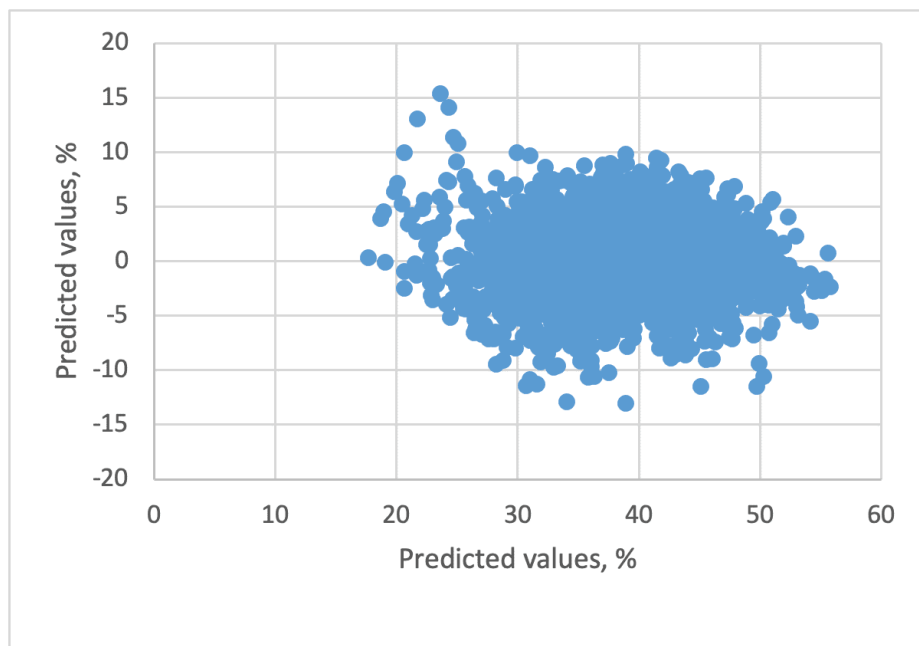
The normal test passed. The residual plots are presented in Figure 4c. A fixed pattern is found at lower predictive values. Although the R^2 , s , and PRESS statistics are a little better than that of the BMI equation, it is not deemed a suitable model.



(a). BMI equation



(b). Ln(BMI) equation



(c). 1/BMI equation

Figure 4. Residual plots of BF equation for black women.

3.2.3. White men and women

The relationship between BF and BMI for white men and women is presented in Figure 5. At the same BMI value, the BF of women is higher than men.

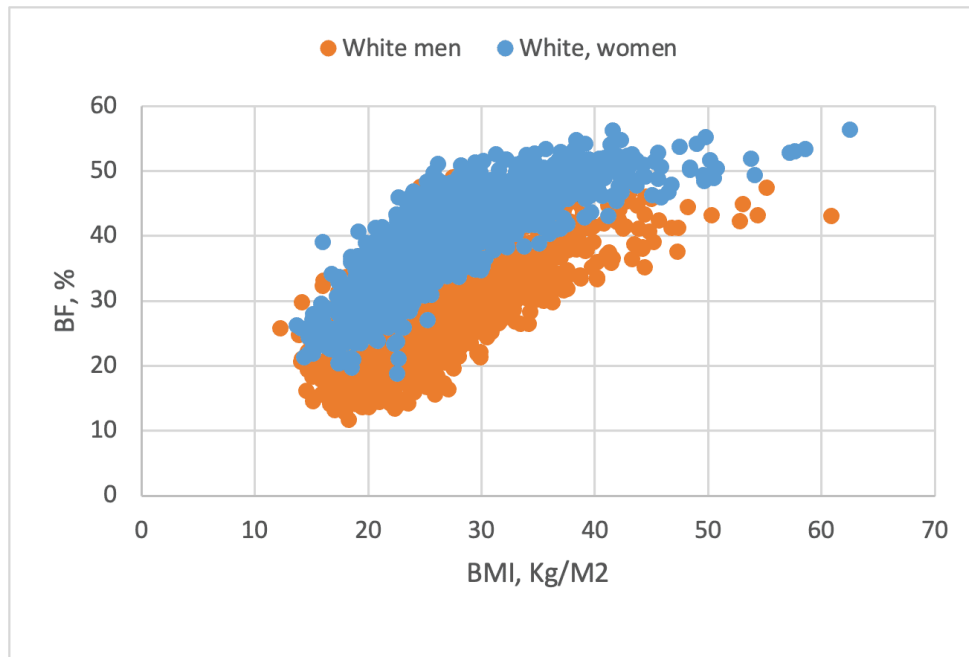


Figure 5. Relationship between BF and BMI for white men and women.

The adequate BF equations are as follows:

White men:

$$BF = -608 + 1.680BMI - 0.0124BMI^2 - 0.411age + 0.00467age^2 \quad (16)$$

$$R^2=0.612, s=4.548, PRESS=44,884$$

White Women:

$$BF = -5.831 + 2.242BMI - 0.0228BMI^2 + 0.0218age + 0.000377age^2 \quad (17)$$

$$R^2=0.766, s=3.501, PRESS=29,147$$

3.2.4. Mexican men and women

The data distribution between BF and BMI for Mexican men and women is presented in Figure 6. The adequate models are listed as follows:

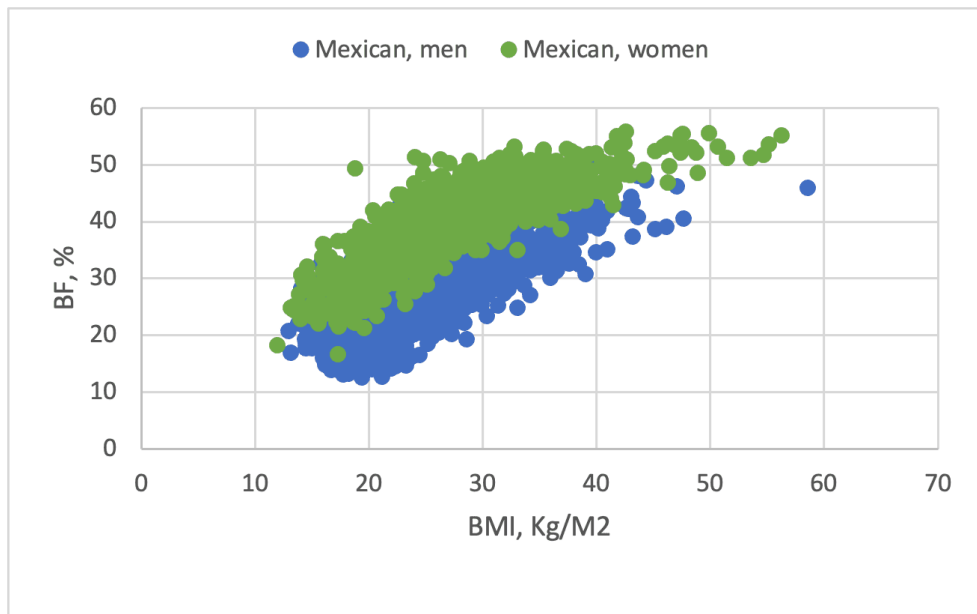


Figure 6. Data distribution between BF and BMI for Mexican men and women.

Mexican men

$$BF = 1.502 + 1.812BMI - 0.0143BMI^2 - 0.661age + 0.00758age^2 \quad (18)$$

$$R^2=0.591, s=4.572, PRESS=45,028$$

$$BF = 21.013 - 16.220\ln BMI + 6.629(\ln BMI)^2 - 0.647age + 0.00745age^2 \quad (19)$$

$$R^2=0.588, s=4.589, PRESS=45,405$$

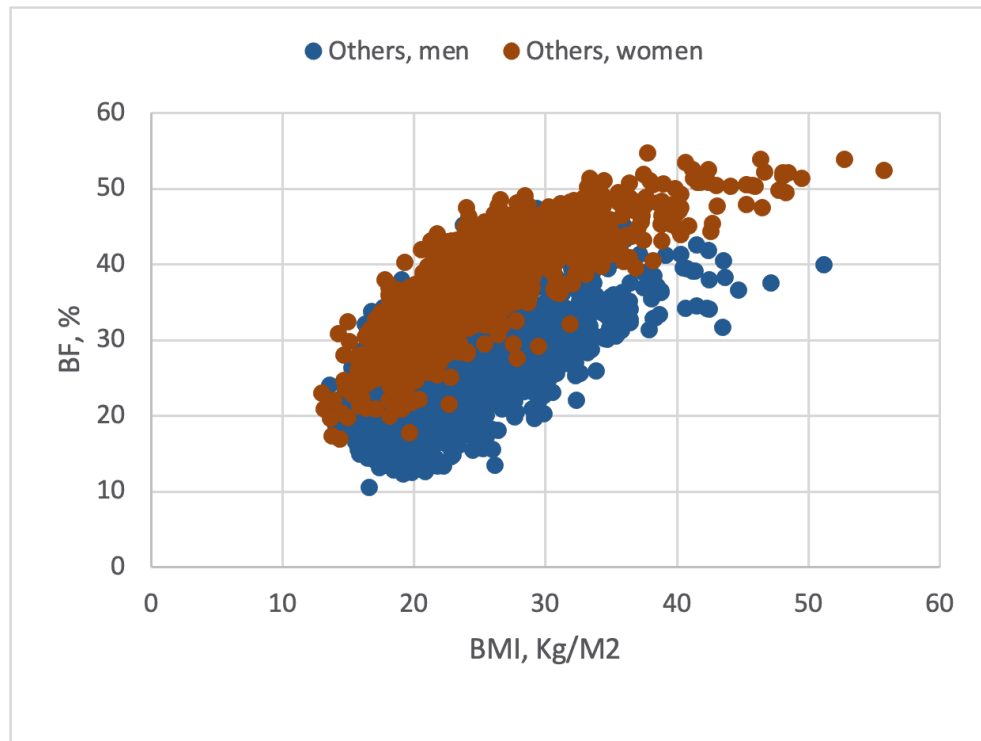
Mexican women

$$BF = 1.322 + 1.941BMI - 0.0191BMI^2 - 0.0387age + 0.00097age^2 \quad (20)$$

$$R^2=0.74, s=3.477, PRESS=27,397$$

3.2.5. Others

The data distribution between BF and BMI for other men and women is presented in Figure 7. The adequate models are:



Men

$$BF = 3.055 + 1.502BMI - 0.0110BMI^2 - 0.478age + 0.00585age^2 \quad (21)$$

$$R^2=0.489, s=4.957, PRESS=25,733$$

$$BF = 30.091 - 21.176\ln BMI + 6.902(\ln BMI)^2 - 0.469age + 0.00577age^2 \quad (22)$$

$$R^2=0.487, s=4.963, PRESS=25,801$$

Women

$$BF = -1.848 + 2.089BMI - 0.0212BMI^2 - 0.02241age + 0.00758age^2 \quad (23)$$

$$R^2=0.722, s=3.715, PRESS=13,004$$

All regression analysis results are listed in Table 4. From the above discussion, the BMI equation could express the relationship between BF and two influence factors (BMI and age) for gender and four ethnicities. The $\ln BMI$ equation can be used for Mexican men and other men. However, its fitting agreement and prediction performance were not better than the BMI equations. The BMI equation was then used for the categorical test.

Criteria Numbers		Black		White		Mexican		Other	
		Men	Women	Men	Wome	Men	Women	Men	Women
		(2286)	(2284)	(2,320)	(2,366)	(2,218)	(2,258)	(1,043)	(938)
BMI	R2	0.626	0.798	0.622	0.766	0.591	0.740	0.489	0.722
	s	4.675	3.731	4.492	3.501	4.572	3.477	4.957	3.715
	PRESS	50,176	31,944	44,884	29,149	45,028	27,397	25,733	13,004
	Normal test	Pass	Pass	Pass	Pass	Pass	Pass	Pass	Pass
	Residual plots	Pass	Pass	Pass	Pass	Pass	Pass	Pass	Pass
Ln BMI	R2	0.613	40.796	0.609	0.766	0.588	0.741	0.487	0.724
	s	4.691	3.756	4.567	3.503	4.589	3.429	4.963	3.705
	PRESS	50,555	32,362	46,876	29,152	45,405	27,441	25,801	12,929
	Normal test	Fail	Pass	Fail	Pass	Pass	Pass	Pass	Pass
	Residual plots	Fail	Fail	Fail	Fail	Pass	Fail	Pass	Fail
1/BMI	R2	0.637	0.799	0.622	0.760	0.599	0.742	0.493	0.725
	s	4.665	3.725	4.494	3501	4529	3468	4.933	3.701
	PRESS	49,682	31,843	47,579	29,121	44,187	37,377	25,491	12,926
	Normal test	Fail	Pass	Fail	Pass	Fail	Pass	Fail	Pass
	Residual plots	Fail	Fail	Fail	Fail	Pass	Fail	Pass	Fail

Table 4. Results of regression analysis of BMI, InBMI, and 1/BMI equations for three ethnicities and gender.

3.3. Categorical test of gender

Black men and women

The BMI equation including the gender effect is:

$$BF = -0.314 - 4.844Z + 1.698BMI - 0.0125BMI^2 + 0.363BMI*Z - 0.00692BMI^2*Z$$

$$(-0.197) (-2.434) (13.765) (-5.944) (2.456) (-2.868)$$

$$- 0.684age + 0.0842age^2 + 0.696z*age - 0.00807age^2*Z$$

$$(-19.851) (19.447) (16.047) (-15.361) (24)$$

Where Z is the categorized variable, Z=0 is men, and Z=1 is women. The t-values involving the parameters are significant. The gender factor had a significant effect on the BF and BMI and the age relationship of black men and women.

White men and women

The data distribution between BF and BMI for white men and women is in Figure 5. The BMI equation, including the gender effect, is:

$$BF = 2.691 - 8.523Z + 1.363BMI - 0.00804BMI^2 + 0.879BMI*Z - 0.0148BMI^2*Z$$

$$(-4.02) (5.732) (-5.858)$$

$$- 0.333age + 0.00398age^2 + 0.355z*age - 0.00361age^2*Z$$

$$(9.824) (-9.902) (25)$$

Where Z is the categorized variable, Z=0 is men, and Z=1 is women. The t-values involving the Z parameters are not equal to zero. Gender had a significant effect on the BMI equation of white people.

Mexican men and women

The BMI equation involving gender factors for Mexican men and women is:

$$BF = -0.513 + 3.302Z + 1.976BMI - 0.0172BMI^2 - 0.148BMI*Z - 0.00471BMI^2*Z$$

$$(4.168) (-4.913) (-1.783)$$

$$- 0.670age + 0.00767age^2 + 0.639z*age - 0.00677age^2*Z^{[26]}$$

The t-values of all parameters involving Z were significant, except the term BMI²*Z. Gender significantly affected the relationship between BF and BMI and age.

Other men and women

The BMI equation involving gender factors for other men and women is:

$$BF = 3.055 - 4.903Z + 1.502BMI - 0.0110BMI^2 + 0.587BMI*Z - 0.0102BMI^2*Z$$

$$(-7.37) (2.703) (-2.710)$$

$$- 0.478age + 0.00585age^2 + 0.455z*age - 0.00509age^2*Z$$

$$(9.790) (-9.411)^{[27]}$$

The t-values of all parameters involving Z were significant, except for the term Z. Gender had a significant effect on the BF value.

From the result of the above discussion, gender is a significant influencing factor on the BF value for four ethnicities: Black, White, Mexican, and others.

3.4. Categorical test of ethnicity

Figures 8 and 9 present the data distribution of BF and BMI for three ethnicities and genders. The significant difference among ethnicities can be observed using the visual method. The categorical test of these data is shown in Table 5.

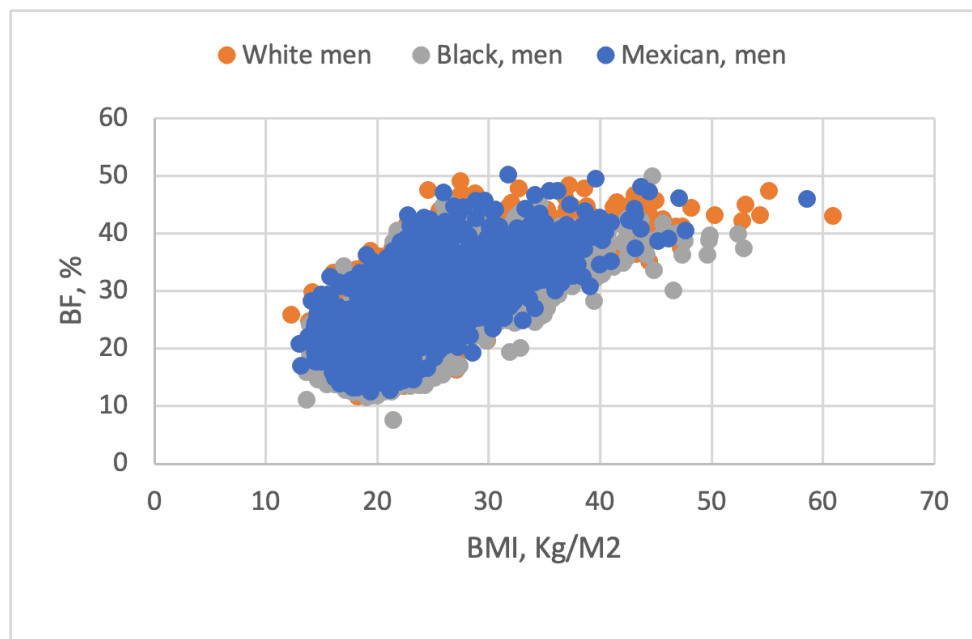


Figure 8. Data distribution of BF and BMI for three ethnicities of men.

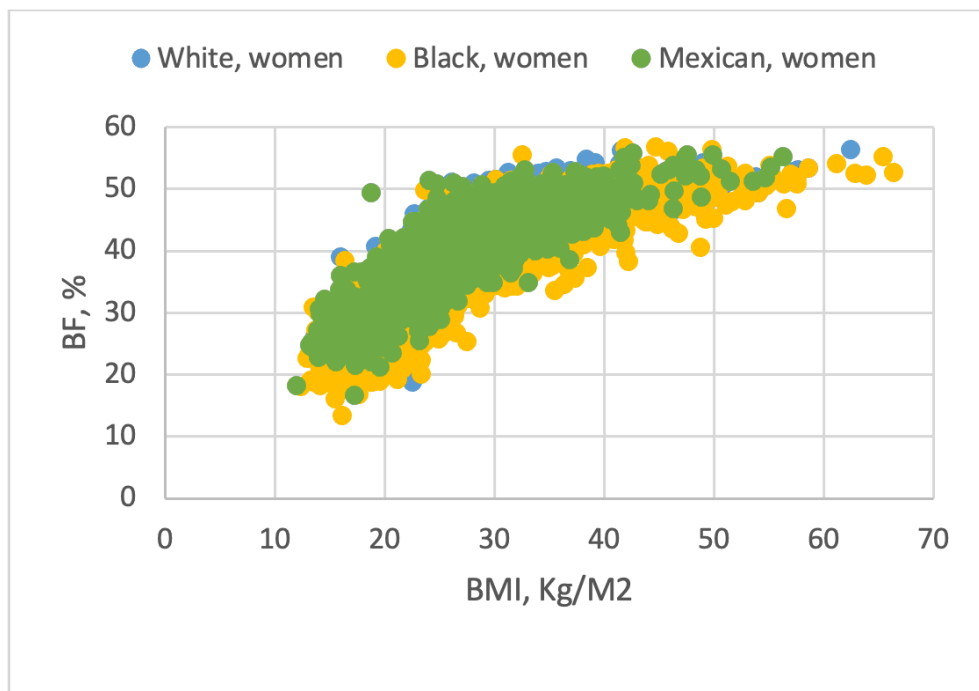


Figure 9. Data distribution of BF and BMI for three ethnicities of women.

Table 5. shows that ethnicity is a significant factor in the BF values.

1. Men, White and Black $BF = 1.064 + 1.482BMI - 0.00997BMI^2 + 0.114BMI * Z - 0.000807BMI^2 * Z - 0.336age + 0.0010age^2 - (2.117) (-0.708) 0.345age * Z + 0.00441age^2 * Z (-7.269) (7.895)$ Where Z=0 is White men, and Z=1 is Black men. The categorical factor (Z) significantly affected BMI, age, and age2 variables.
2. Women, White and Black $BF = -5.846 + 0.974Z + 2.266BMI - 0.0231BMI^2 - 0.2278BMI * Z + 0.00402BMI^2 * Z + 0.00989 age + 0.000450 age^2 (-2.811) (2.467)$ Where Z=0 is White women, and Z=1 is Black women. Ethnicity had a significant effect on BMI and BMI2 variables. However, it did not significantly affect age and age2 variables.
3. Men, White and Mexican $BF = 0.397 + 3.298Z + 1.545BMI - 0.0111BMI^2 + 0.889BMI * Z - 0.343age + 0.00407age^2 - 0.308age * Z + 0.00344age^2 * Z (3.72) (2.476) (-7.119) (6.951)$ Where Z=0 is White men, and Z=1 is White Mexican. The categorical factor Z significantly affected intercept, BMI, age, and age2 variables.
4. Women, White and Mexican $BF = -5.603 + 7.070Z + 2.267BMI - 0.0231BMI^2 - 0.367BMI * Z + 0.00456BMI^2 * Z - 0.00784age + 0.000651age^2 (4.091) (-3.146) (2.293)$ Where Z=0 is White women, and Z=1 is Mexican women. The categorical factor significantly affected intercept, BMI, and BMI2. However, there was no significant effect on the age and age2 variable.
5. Men, Mexican, and Others. $BF = 11.383 + 8.323Z + 1.009BMI - 0.0031BMI^2 + 0.493BMI * Z - 0.0119BMI^2 * Z (4.091) (3.146) (2.293) - 0.614age + 0.00714age^2 - 0.138age * Z + 0.0013age^2 * Z (-2.765) (-2.178)$

Where Z=0 is Mexican men, and Z=1 is other men. Ethnicity significantly affected intercept, BMI, BMI2, age and age2 .
6. Women, Mexicans and others $BF = 0.230 + -0.615Z + 2.001BMI - 0.0199BMI^2 + 0.0302age + 0.000864age^2$ (-3.955) where Z=0 is Mexican women, and Z=1 is other women. Ethnicity only had a significant effect on intercept.

Table 5. Results of categorical test of BF and BMI and age equations for different ethnicities.

3.5. Categorical test of ethnicity and gender

In this categorical test, a more complex equation (Equation 6) was proposed to consider the effect of ethnicity and gender simultaneously. The factor of ethnicity included three races: Black, Mexican, and White. The sample number of others is limited, so this study did not use the data set. The results of the regression analysis are listed in Table 6.

$BF = 4.538 + 8.277 * z1 + 6.685 * z2 + 1.375 * z3 + 0.818 * BMI - 0.741 * z1*BMI - 0.442 * z2*BMI + 0.691 * z3*BMI + 0.000118 * BMI^2 + 0.0127 * z1*BMI^2 + 0.00737 * z2*BMI^2 - 0.0117 * z3*BMI^2 + 0.0759 * age - 0.0249 * z1*age - 0.109 * z2*age - 0.134 * z3*age - 0.000183 * age^2 + 0.0000113 * z1*age^2 + 0.00119 * z2*age^2 + 0.00140 * z3*age^2$					
Coefficient	Std. Error	t	P		
Constant	4.538	0.343	13.242	<0.001	
z1	8.277	0.293	28.269	<0.001	
z2	6.685	1.607	4.160	<0.001	
z3	1.375	1.118	1.229	0.219	
BMI	0.818	0.0124	66.187	<0.001	
z1*BMI	-0.741	0.0473	-15.677	<0.001	
z2*BMI	-0.442	0.119	-3.712	<0.001	
z3*BMI	0.691	0.0806	8.573	<0.001	
BMI^2	0.000118	0.000390	0.303	0.762	
z1*BMI^2	0.0127	0.000937	13.594	<0.001	
z2*BMI^2	0.00737	0.00201	3.664	<0.001	
z3*BMI^2	-0.0117	0.00133	-8.753	<0.001	
age	0.0759	0.00388	19.535	<0.001	
z1*age	-0.0249	0.0323	-0.771	0.441	
z2*age	-0.109	0.0316	-3.448	<0.001	
z3*age	-0.134	0.0261	-5.136	<0.001	
age^2	-0.000183	0.0000736	-2.486	0.013	
z1*age^2	0.0000113	0.000347	0.0325	.974	
z2*age^2	0.00119	0.000364	3.265	0.001	
z3*age^2	0.00140	0.000286	4.887	<0.001	

Table 6. The results of the categorical test of the BMI equation for three ethnicities and gender.

The results of Table 6 indicated that ethnicity and gender both significantly affect the intercept, BMI, BMI², age, and age².

The categorical factors, ethnicity, and gender significantly affect the BMI equations. No single form of the BF equation could be proposed to present the relationship between BF, BMI, and age. Each ethnicity of men or women must have its specific BMI equation.

From the above result, all R² values of female subjects are higher than those of male subjects for the same ethnicity. That is, the variation in BF values could be better explained by BMI and age for women than men. Gender has a significant effect on BF values. At the same BMI value, the BF value of female subjects is higher than that of male subjects.

4. Discussion

In this study, an adequate BF equation is $BF = b_0 + b_1BMI + b_{11}BMI^2 + b_2age + b_{22}age^2$. The interaction of BMI and age did not significantly affect the BF value. This model's evaluation includes the normality and constant variance test. All variables were validated using the t-values and p-values of each estimated value of the parameters. After an adequate BF model was established, the effects of sex and ethnicity were tested using a categorical test.

Researchers have studied many forms of BF equations. The simple linear equation validates the narrow BMI range^{[6][12][39]}. When the BMI value is >35 kg/m², nonlinear or polynomial equations have been proposed^{[4][11]}. Categorical variables such as gender have been incorporated into simple linear equations^{[7][39]}. However, an adequate BF equation was not evaluated in advance. The selection criteria are limited by the classical regression technique, such as R² and s.

Most of the literature used R² and s as the criteria to evaluate the fitting agreement of their model. Only some literature mentioned the p-values test to validate the significance of each estimated variable value^{[8][11][16][19]}.

Some reports did not test the basic assumptions of the normal distribution and constant variance. The residual plots were only reported by Levitt et al.^[4] and Fuster-Parra et al.^[18]. In the study of Levitt et

al.^[4], a funnel-type distribution of residuals was found for their nonlinear model, and a fixed pattern of under-estimation was found as BMI > 40 kg/m². Fuster-Parra et al.^[18] proposed a complex form of the BF equation, and log BMI was used as a variable. The residual plots of men and women subjects all revealed a funnel-type distribution. When the BMI > 40 kg/m², the fixed pattern indicated the predicted values were under-estimated.

The effect of the age variable on the BF value was assumed to be the variable of age in the BF equation^{[4][7][8]}. Only the equation proposed by Meeuwsen et al.^[16] considered the power term of age². However, in our study, the variable of age² should be incorporated into the BF equation for all ethnicities and both genders.

Meeuwsen et al.^[16], Gomze-Ambrosi et al.^[17], and Fuster-Parran et al.^[18] have introduced complex multiple regression equations. In the study of Merrill et al.^[40], four anthropometric measurements—waist circumference, hand thickness, vertical abdominal skinfold, and thigh skinfold—were adopted as the dependent variables. However, the multicollinear tests of these variables were not reported.

The modern regression technique has been used to predict liver volume^[41], evaluate the environmental factor on the growth of plantlets in plant tissue culture^[42], find the influencing factors on honey properties^[43], and evaluate the influencing factors on the dielectric properties of foods^[44]. Regression equations with a categorical test could determine which factors significantly affect the BF values. In this study, the significant effects of gender and ethnicity on the BF values are validated with the categorical test of regression analysis. This method can be applied to other data sets of BF, BMI, and other factors to classify these quantitative and qualitative factors.

Faradisa et al.^[37] adopted fuzzy logic to establish the relationship between BF and BMI and found that BF and BMI can produce the same categories. However, only classification methods cannot meet the medical requirements for the application of BF values in diagnosis. Xu et al.^[38] used a supervised machine learning technique to develop the prediction equation for BF and BMI and the best model included 18 variables and 19 parameters. The selection of the variables in the prediction equations were evaluated by algorithm, a block box for data analysis. There is no academic basis for judging which variables are suitable to be retained in the empirical formula. The best equation proposed by the author is derived from the most selected variables but failed to test whether the impact of these variables on BF is significant. In this study, the significant effect for each variable is tested by t-test

and the predictive performance is evaluated with the PRESS statistics. These methods have their academic basis in Mathematics and Statistics.

Recently, the BF prediction equation with BMI and other factors still be concerned by researchers. The calculation of the BF values with the BMI and other variables is a simple way. The prediction ability of the BF empirical equations have been concerned with researchers and clinicians. With the study of BF prediction in older adults, Silveria et al.^[45] suggested to develop specific equations for older adults and the age variables in their application equations did not considering the age and age² terms. Marin-Jimenez et al.^[46] reviewed several BF prediction equations and found the BF calculation equation with anthropometric methods can support a simple and easy indicators and the specific population equations considered the age and each should be considered in these equations. Sweatt et al.^[47] discussed the strengths and limitations of BMI in the diagnosis of obesity and recommended some anthropometrics such as waist circumference and waist to height ratio to be considered in the BF equations. However, no empirical equations were reported. Takeyama and Fujii^[48] recommended that the BF values should consider the effect of height difference of tall, medium, and short. They proposed three BF linear equations and the effect of the heights did not be incorporated in these equations. Taylor et al.^[49] report a BF circumference-based equations included the sizes of the abdomen, hip, waist, weight and height. However, they did not report the statistics of regression equation. Wu et al.^[50] reviewed the advantages and limitations of the application of the BMI to evaluate the adult obesity, and confirmed that the BMI value is valuable for the primary healthcare screening and limited to serve as the predicting of chronic diseases and excess fat assessment. In this study, BF equations have considered the effect BMI, age, gender, and race. The prediction equations developed in this study could be enhance the application of the BMI value with considering other factors.

In our study, humans' BF values are affected by their BMI, BMI², age, age², gender, and ethnicity. No single form of the BF equation can be proposed, and cut-off values for BF cannot be selected as fixed values for humans. The modern regression technique used in this study can be applied to other data sets to establish the adequate BF prediction equation. Then the calculating BF values could serve as an index for the primary healthcare screening. With an adequate prediction BF equation, this simple method of the BF calculation with weight, height, and other factors is very helpful for public health management.

For the future research, the exploring additional anthropometric measures or investigating more complex interactions between factors like physical activity level and body fat prediction, could be provided a broader perspective on the prediction of the BF values.

5. Conclusion

Percent body fat (BF) can serve as an index for human health conditions. A simple predictive equation to calculate the BF value by the influencing factors is very useful. Many empirical equations have been proposed, and inconsistent results have been found. In this study, four data sets, including gender and four ethnicities—white, Black, Mexican, and others—were used to ascertain an adequate BF equation.

The criteria for assessing the appropriate equations used classical regression techniques in previous studies, such as the coefficient of determination, R^2 , and the estimation value of standard errors, s . In this study, the modern regression technique was used to evaluate the significant effect of each variable with t-test and the predictive performance with PRESS statistics. The effect of other factors such as age, gender, and ethnics was evaluated with categorical testing.

The results of this study indicate the best model of BF uses BMI, BMI², age and age² variables. Categorical tests tested the effects of gender and ethnicity on the BF value, and all had a significant effect on BF values. Using a universal BMI equation for all ethnicities or genders is inappropriate. By calculating the BMI value, the cutoff point of BF values needs to consider the difference between gender and ethnicity. This technique in this study provides a reasonable method to establish a BF equation for different age, gender, and ethnicities.

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