

Peer Review

Review of: "Primary Hairs May Create Echoes"

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Looking at the conclusion, it is surprising that the modified terms in the Lagrangian and the scalar, vector, and Dirac fields from primary Proca-Gauss-Bonnet hair themselves, in the exterior region of any spherically static stars, can provide another barrier located near the horizon and enveloped by the usual potential barrier near the photon--sphere. This is due to certain choices of α and β . I can see in Fig. 3 that the inner bump is small compared to the main outer bump, and the distance can be quite far from each other, hence producing a relatively small echo frequency.

I need to clarify some things as follows.

1. Because I see some choices of α s, β s, and fields (scalar and Dirac), I cannot easily see the difference in their respective results. Can you explain concisely how different choices of α and β impact the results and echo frequencies? At least in the conclusions, perhaps write it in a table for convenience.
2. There are some things that need to be addressed related to the frequency result. In Fig. 3, upper row on the right, what l (lowercase L) is used in the potential shown there? $l=0$, $l=1$, or else? Perhaps adding more plots for comparing potentials from different l values would be beneficial. Moreover, another table for results from $l=1$ may be needed just like Table 1 so that anyone can see the difference in numerical values between $l=0$ and $l=1$.
3. The eikonal parameter ϵ is a bit unclear in its relation to Eq. 15. Also, how exactly can the eikonal parameter correct the value of the frequency? I apologize if this question is a bit naive, but I think the clarity regarding the numerical steps needs improvement.

Declarations

Potential competing interests: No potential competing interests to declare.